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Abstract— This paper proposes a linearized large signal state-space model for the fixed-frequency phase-controlled series-parallel resonant converter. The proposed model utilizes state feedback of the output filter inductor current to perform linearization. The model combines multiple-frequency and average state-space modeling techniques to generate an aggregate model with dc state variables that are relatively easier to control and slower than the fast resonant tank dynamics. The main objective of the linearized model is to provide a linear representation of the converter behaviour under large signal variation which is suitable for faster simulation and large signal estimation/calculation of the converter state variables. The model also provides insight into converter dynamics as well as a simplified reduced order transfer function for PI closed loop design. Experimental and simulation results from a detailed switched converter model are compared with the proposed state-space model output to verify its accuracy and robustness.

Index Terms— Large signal, phase control, series-parallel resonant converter (SPRC), state feedback.

I. INTRODUCTION

DC/DC power converters are employed in a variety of applications, including power supplies for computers, office equipment, spacecraft power systems, laptop and telecommunications equipment, as well as dc motor drives. This is achieved using switched-mode PWM, or resonant-mode converters which allow control and regulation of the output voltage. Nowadays dc/dc converters are a common technology for renewable energy source grid integration [1,2], dc microgrids [3], HVDC systems [4], offshore oil and gas systems [5] in addition to interfacing energy storage elements such as batteries in UPS systems [6].

Dc/dc resonant converters are an alternative to hard-switched PWM converters in dc power supply applications. This is due to their soft switching characteristics; hence give the possibility of boosting the switching frequency and

NOMENCLATURE

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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<tbody>
<tr>
<td>$v_s$</td>
<td>DC link supply voltage (V)</td>
</tr>
<tr>
<td>$v_{AB}$</td>
<td>Inverter output voltage (V)</td>
</tr>
<tr>
<td>$n$</td>
<td>Transformer turns ratio</td>
</tr>
<tr>
<td>$v_{AB}$</td>
<td>Inverter output voltage referred to transformer secondary = $nv_{AB}$ (V)</td>
</tr>
<tr>
<td>$r_{Ls}$</td>
<td>Internal resistance of resonant tank inductor ($\Omega$)</td>
</tr>
<tr>
<td>$L_s$</td>
<td>Resonant tank inductance ($\mu$H)</td>
</tr>
<tr>
<td>$r_l$</td>
<td>Parasitic resistance of transformer referred to secondary ($\Omega$)</td>
</tr>
<tr>
<td>$L_l$</td>
<td>Leakage inductance of transformer referred to secondary ($\mu$H)</td>
</tr>
<tr>
<td>$r_T$</td>
<td>Total equivalent resistance ($\Omega$)</td>
</tr>
<tr>
<td>$L_T$</td>
<td>Total equivalent inductance ($\mu$H)</td>
</tr>
<tr>
<td>$C_s$</td>
<td>Resonant tank series capacitance ($\mu$F)</td>
</tr>
<tr>
<td>$C_p$</td>
<td>Resonant tank parallel capacitance ($\mu$F)</td>
</tr>
<tr>
<td>$r_{Lo}$</td>
<td>Internal resistance of output filter inductor ($\Omega$)</td>
</tr>
<tr>
<td>$L_o$</td>
<td>Output filter inductance (mH)</td>
</tr>
<tr>
<td>$C_o$</td>
<td>Output filter capacitance ($\mu$F)</td>
</tr>
<tr>
<td>$\omega_s$</td>
<td>Resonant tank fundamental frequency (rad/s)</td>
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<tr>
<td>$i_L$</td>
<td>Resonant tank inductor current (A)</td>
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<td>$v_{Cs}$</td>
<td>Resonant tank series capacitor voltage (V)</td>
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<td>$v_{Cp}$</td>
<td>Resonant tank parallel capacitor voltage (V)</td>
</tr>
<tr>
<td>$i_{Br}$</td>
<td>Bridge rectifier input current (A)</td>
</tr>
<tr>
<td>$v_{Br}$</td>
<td>Bridge rectifier output voltage (V)</td>
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<tr>
<td>$\bar{v}_{Br}$</td>
<td>Average bridge rectifier output voltage (V)</td>
</tr>
<tr>
<td>$i_{Lo}$</td>
<td>Output filter inductor current (A)</td>
</tr>
<tr>
<td>$v_o$</td>
<td>Output voltage (V)</td>
</tr>
<tr>
<td>$i_o$</td>
<td>Output current (A)</td>
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reducing the transformer and filter size and weight. However, this is usually a design trade-off with the relatively high resonant peak voltages and currents.

Several types of resonant converters have been applied in dc power supply applications. Series resonant converters have poor no-load regulation, poor short circuit characteristics and need a larger output filter capacitor [7-9]. However its switching losses decrease with load decrease. They are suitable for high-output-voltage low-output-current converters [10-13]. Parallel resonant converters [14-16] have better no-load regulation and are naturally short circuit proof due to the resonant tank inductor. However, high circulating resonant tank current means higher switching losses and the converter is better suited to applications with a relatively narrow input voltage range. The combination series-parallel resonant converter (SPRC) combines advantages of both and eliminates their drawbacks. It can operate over a large input voltage range and a large load range (no load to full load) while maintaining high efficiency [17-20]. For this reason, this paper focuses on application of the SPRC in dc power supplies.

Various control techniques have been used to control resonant converters. These can be broadly classified into variable frequency and fixed-frequency approaches. Variable frequency techniques include average-current control, frequency control, capacitor voltage control, diode-conduction-angle control, and optimal trajectory control [20-22]. However, these variable frequency techniques present practical disadvantages, like a wide noise spectrum which make it difficult to control EMI, more complex filtering is needed, and poor utilization of magnetic components. Also, the frequency control range is limited if zero voltage switching (ZVS) of the converter is to be achieved. Operation below resonance means ZVS is lost and the inverter switches operate with turn on losses. This necessitates the use of fast recovery anti-parallel diodes to avoid diode recovery shoot-through within the same inverter leg. Operation above resonance is preferred where the SPRC operates with lagging power factor, hence ZVS. However, an increase in switching frequency above resonance results in a large non-linear reduction in converter voltage gain. Therefore, if frequency control is to be implemented, a narrow range of frequency control above resonance is necessary to achieve both ZVS and an acceptable voltage gain. Fixed frequency control above resonance such as phase shift control [23-25] overcomes the problems of variable frequency control and offers good control of the output voltage by controlling the phase-shift angle between the inverter legs; hence the effective inverter output voltage duty-cycle ratio. For the aforementioned reasons, this paper focuses on fixed frequency phase control of a SPRC.

Modeling of resonant converters is more complex than PWM converters. This is mainly due to the non-linear coupling of its ac and dc state variables. Various modeling techniques have been proposed in literature for the SPRC. Steady-state operation has been analyzed [18, 26-30], providing good insight into converter behavior and overall steady state gain. Small signal models for the SPRC use linearized state-space models around an equilibrium point to enable stability analysis and closed loop design [31]. The resulting closed loop design, although eliminating error in the output voltage, results in an unsatisfactory dynamic response. Small signal models include discrete time domain [32-34] and multiple frequency techniques [35-37]. A method based on discrete time domain modeling has been proposed for low order converters. It becomes cumbersome with higher order converters. The multiple frequencies method transforms ac signals into dc signals at multiple frequencies, thereby providing a theoretically high accuracy model [38]. Although small signal model is sufficient for analysis and closed loop design, it cannot be used to estimate converter state variables under large signal variations, which is possible if the converter is operating with a wide range input voltage or variable load. Large signal models based on a describing function method have also been proposed for SPRC analysis [39,40]. However, due to model non-linearity, non-linear controllers such as the sliding mode technique [41,42] and robust optimal control [43] were designed for SPRC control.

In this paper, a linearized large signal model for the SPRC is obtained using a state feedback scheme. The latter utilizes measurement of the output filter inductor current to perform model linearization. The model is useful for faster simulation as well as large signal estimation/calculation of converter ac and dc state variables, which can be used for converter sensorless control. In section two, the non-linear nature of resonant converters is explained. An aggregate SPRC large signal model is derived in section three. In section four, the state feedback scheme necessary for linearization is introduced. More analysis is performed on the linearized system model in section five. Finally, the accuracy and robustness of the model are assessed and validity by comparing experimental and MATLAB simulation results, using a detailed switching model of the phase-controlled SPRC.

II. NON-LINEAR NATURE OF DC/DC RESONANT CONVERTERS

Fig. 1 shows the circuit diagram for a typical SPRC. The bridge rectifier, together with the output LC filter, act as a non-linear load to the resonant tank circuit. This non-linearity is clarified in Fig.2. Hence, the converter large signal response cannot be modeled using linear approaches such as conventional average state-space models.

![Fig. 1. Circuit diagram for the SPRC.](image-url)
III. PROPOSED MODEL FOR THE DC/DC RESONANT CONVERTER

DC/dc resonant converters have two stages of conversion; dc/ac (inversion) and ac/dc (rectification). Hence, two main subsystems exist; the ac sub-system (resonant tank and transformer) and the dc sub-system (output filter), as illustrated in Fig. 3. Each sub-systems has its own state variables; therefore, both ac and dc state variables exist. In order to combine both types of signals into one model, it is essential to transform the ac state variables to equivalent dc quantities. This is achieved with the multiple frequency modeling (MFM) technique which converts the ac state variables to d-q quantities (dc values with slow dynamics) using an arbitrary synchronous reference frame. The resulting dc state variables from the resonant tank are combined with the natural dc state variables of the output filter side (modeled with conventional average state-space modeling) using a linearization scheme to overcome the non-linearity imposed by the rectifier. The result is an aggregate large signal linear model for the complete converter.

A. Ac sub-system modeling

Fig. 4 shows the equivalent circuit diagrams for the ac sub-system of the SPRC. Three state variables exist: \( i_L, v_{Cs}, v_{Cp} \). The voltage-current relations are described by equations (1) to (3).

\[
\begin{align*}
v_{Ab} &= r_L i_L + L_T \frac{di_L}{dt} + v_{Cs} + v_{Cp} \\
i_L &= C_s \frac{dv_{Cs}}{dt} \\
i_L - i_{Br} &= C_p \frac{dv_{Cp}}{dt}
\end{align*}
\]

The multiple frequency modeling approach [35,36] for the SPRC, is utilized to model the ac sub-system of the resonant converter. Since the state variables have periodic characteristics, each state can be expressed by a Fourier series [37,38]. Energy transfers from the input to the output mainly at the fundamental frequency, hence the dominant frequency for modeling and analysis of the ac sub-system state variables is assumed to be \( \omega_s \), the operating frequency of the converter.

The state variables and input can be approximated as sinusoidal states with fundamental frequency \( \omega_s \) as in equations (4) to (8).

\[
\begin{align*}
i_L &= i_{Ld} \sin \omega_s t + i_{Lq} \cos \omega_s t \\
v_{Cs} &= v_{Cs d} \sin \omega_s t + v_{Cs q} \cos \omega_s t \\
v_{Cp} &= v_{Cp d} \sin \omega_s t + v_{Cp q} \cos \omega_s t \\
v_{Ab} &= v_{Ab d} \sin \omega_s t + v_{Ab q} \cos \omega_s t \\
i_{Br} &= i_{Br d} \sin \omega_s t + i_{Br q} \cos \omega_s t
\end{align*}
\]

where \( i_{Ldq}, v_{Csdq} \) and \( v_{Cpdq} \) are time-varying Fourier coefficients. These six Fourier coefficients, being time-dependent dc quantities, are considered as the new set of state variables. \( v_{Abd}, v_{Abq}, i_{Brd} \) and \( i_{Brq} \) are time-varying Fourier coefficients representing the new set of inputs to the model. Substituting equations (4)-(8) into equations (1)-(3), and equating sine and cosine coefficients, yields

\[
\begin{align*}
v_{Abd} &= r_L i_{Ld} + L_T \frac{di_{Ld}}{dt} - L_T \omega_s i_{Lq} + v_{Csd} + v_{Cpd} \\
v_{Abq} &= r_L i_{Lq} + L_T \frac{di_{Lq}}{dt} + L_T \omega_s i_{Ld} + v_{Csq} + v_{Cpq} \\
i_{Ld} &= C_s \frac{dv_{Csd}}{dt} - C_s \omega_s v_{Csq} \\
i_{Lq} &= C_s \frac{dv_{Csd}}{dt} + C_s \omega_s v_{Csq} \\
i_{Ld} - i_{Brd} &= C_p \frac{dv_{Cpd}}{dt} - C_p \omega_s v_{Cpq} \\
i_{Lq} - i_{Brq} &= C_p \frac{dv_{Cpd}}{dt} + C_p \omega_s v_{Cpq}
\end{align*}
\]
Equations (9)-(14) in state-space form:

\[ \dot{x}_i(t) = A_i \bar{x}_i(t) + B_i \bar{u}(t) \]  

where

\[ \bar{x}_i(t) = [i_{Ld} \ i_{Lq} \ v_{Csd} \ v_{Csq}]^T, \quad \bar{u}_i(t) = [v_{ABd} \ v_{ABq} \ i_{Brd} \ i_{Brq}]^T, \]

\[ A_i = \begin{bmatrix} \frac{r_i}{L_r} & -\omega_c & 0 & \frac{1}{L_r} \\ -\omega_c & \frac{r_i}{L_r} & 0 & \frac{1}{L_r} \\ \omega_c & 0 & \frac{1}{C_r} & 0 \\ 0 & -\omega_c & 0 & \omega_c \end{bmatrix}, \quad B_i = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \]

B. Dc sub-system modeling

Fig. 5 shows the equivalent circuit diagram for the SPRC dc sub-system. Note that \( v_{Br} \) is the average rectifier output voltage \( v_{Br} \). Energy is transferred at dc frequency, so the dominant component for modeling and analysis is the dc (average) value. For this reason, average state-space modeling, with a small-ripple assumption, is valid for modeling the dc sub-system.

Two state variables exist (\( i_{Lo} \) and \( v_o \)), for which the voltage-current relationships are described by (16) and (17). The bar notation denoting the average value of the state variables will be neglected for standardization of the model.

\[ v_{Br} = r_{Lo} i_{Lo} + L_o \frac{di_{Lo}}{dt} + v_o \]  

\[ i_{Lo} - i_o = C_o \frac{dv_o}{dt} \]  

Equations (16) and (17) can be used to represent the dc sub-system in state-space form

\[ \dot{x}_2(t) = A_2 \bar{x}_2(t) + B_2 \bar{u}(t) \]

where

\[ \bar{x}_2(t) = [i_{Lo} \ v_o]^T, \quad \bar{u}_2(t) = [v_{Br} \ i_{Lo}]^T, \quad A_2 = \begin{bmatrix} \frac{r_o}{L_o} & -1 \\ 1 & 0 \end{bmatrix}, \quad B_2 = \begin{bmatrix} 0 \\ -1 \end{bmatrix} \]

C. Combined system non-linear model

Fig. 6 shows the non-linear model for the SPRC combining the state-space linear models of the ac and dc sub-systems. The voltage-current relationship between both sub-systems (separated by the bridge rectifier) is outlined by

- The state-variables of the ac sub-system are approximated as sinusoidal at the fundamental frequency, therefore

\[ v_{Br} = \frac{2}{\pi} v_{Br \text{ peak}} = \frac{2}{\pi} v_{Cp \text{ peak}} = \frac{2}{\pi} \sqrt{v_{Cpd}^2 + v_{Cpq}^2} \]  

- Power balance theory: Output power from the ac sub-system is equal to input power to the dc sub-system (assuming lossless rectifier reverse recovery)

\[ \frac{1}{2} (v_{Cpd}^2 + v_{Cpq}^2) = v_{Br}^2 L_o \]

Substituting (19) into (20) yields

\[ \sqrt{v_{Cpd}^2 + v_{Cpq}^2} = \sqrt{v_{Cpd}^2 + v_{Cpq}^2} = \frac{4}{\pi} L_o \]

As outlined by the analysis in [18], it can be also concluded that

\[ i_{Br \text{ peak}} = \frac{4}{\pi} i_{Lo} = \sqrt{v_{Br}^2 + v_{Br}^2} \]

Equations (21) and (22) confirm the non-linear relationship between the ac and dc sub-systems of the series-parallel resonant converter. Hence the voltage-current relationship can be represented by

\[ i_{Bd} = f \left( i_{Lo}, v_{Cpd}, v_{Cpq} \right) \]

\[ i_{Brq} = f \left( i_{Lo}, v_{Cpd}, v_{Cpq} \right) \]

IV. STATE FEEDBACK AND LINEARIZATION

In this section, linear state feedback is used to linearize the relationship between the ac and dc sub-systems of the SPRC. The main objective of this linearization scheme is to formulate the necessary input voltages \( v_{ABd} \) and \( v_{ABq} \) to the resonant tank in Fig. 6 which force either outputs from the resonant tank \( (v_{Cpd} \text{ or } v_{Cpq}) \) to be zero. In this case, the mathematical square-root relationship representing the diode rectifier reduces to a simple gain and both the ac and dc subsystems are cascaded linear systems that can be combined into one aggregate linear model. In order to realize this state feedback scheme, steady-state ac analysis of the resonant tank is performed to calculate the required input voltages \( v_{ABd} \) and \( v_{ABq} \). This is studied in the next sub-section and it is found that a measurement of the output filter inductor current is necessary to realise this linearization scheme.

A. Steady state analysis of ac sub-system

Fig. 7 shows the steady state phasor diagram analysis for the ac sub-system (resonant tank), assuming sinusoidal state variables. The capital notation denotes steady state values. Starting with \( v_{Cp} \) and \( i_{Br} \) and working backwards (as from Fig. 4), the inverter voltage \( v_{AB} \) (referred to secondary) can be expressed as

![Fig. 5. Equivalent circuit diagram for the dc sub-system.](image-url)
Expressions for the steady-state parallel capacitor voltage \( V_{Cp} \) can be obtained by solving (24) and (25) simultaneously and re-arranging

\[
V_{Cp} = \frac{k}{k_k - k_{k_k}} V_{av} - \frac{k}{k_k - k_{k_k}} V_{av} + k_k - k_{k_k} I_{brd} + k_{k_k} - k_k I_{aq}
\]

Therefore, steady state values for the ac sub-system outputs \( V_{Cpd} \) and \( V_{Cpq} \) are obtained as a function of the inputs \( V_{ABd} \) and \( V_{ABq} \). This could be alternatively analyzed using state-space equation (15) at steady-state

\[
0 = A_2 \tilde{X}_2 + B_2 \tilde{U}
\]

**B. State feedback scheme**

The main objective of the linearization scheme is to calculate the necessary input voltages to the resonant tank \( V_{ABd} \) and \( V_{ABq} \) to force either outputs \( V_{Cpd} \) or \( V_{Cpq} \) to zero, in order to circumvent the square-root non-linearity. Choosing either to be zero does not affect the modeling process as the objective is to control the converter output voltage. In this paper, \( V_{Cpq} = 0 \). According to [18], the equivalent ac resistance at the rectifier input is given by

\[
R_e = \frac{\pi^2}{8} R_l
\]

This means that if \( V_{Cpq} = 0 \), then it is also valid that \( I_{brd} = 0 \) due to the resistive relationship. According to (19)-(22), it also becomes true that \( \bar{\omega}_r = 2 / \pi V_{Cpd} \) and \( \bar{\omega}_q = 4 / \pi I_{brd} \). Substituting \( V_{Cpq} = 0 \) and \( I_{brd} = 0 \) into equations (26) and (27), and solving for \( V_{ABd} \) and \( V_{ABq} \) yields

\[
V_{ABd} = k_1 V_{Cpd} + k_2 I_{brd}
\]

\[
V_{ABq} = k_3 V_{Cpd} + k_4 I_{brd}
\]

Equations (31) and (32) show that the resonant circuit input voltage \( V_{AB} \) is a function of \( I_{brd} \) (proportional to the load current) and \( V_{Cpd} \) (proportional to the output voltage). \( V_{AB} \) has to follow the relationship outlined by (31) and (32) in order to satisfy the main criteria for linearizing the converter model \( (I_{brd} = 0 \) and \( V_{Cpq} = 0 \)) and to ensure stable converter operation. The ac sub-system (resonant tank) is fed with
An aggregate model for the resonant converter can be obtained by combining the two linear state-space models in (15) and (18) for the ac and dc sub-systems respectively. Taking the relationship in (35) into account, yields the aggregate model in (36),

\[
v_{\text{ab}} = \frac{2}{\pi} v_{\text{cd}} + i_{\text{bd}} = \frac{4}{\pi} i_{\text{o}}^*, i_{\text{dq}} = 0 \]

where \( v_c \) is a common control input for control of the converter output voltage. This scheme uses a weighted state feedback approach to linearize the resonant converter model. The weighted feedback is implemented using the output filter inductor current \( i_{\text{o}} \) as shown in Fig. 8.

**C. Aggregate linear model**

An aggregate model for the resonant converter can be obtained by combining the two linear state-space models in (33) and (37) for the ac and dc sub-systems respectively. Taking the relationship in (35) into account, yields the aggregate model in (36),

\[
\begin{align*}
\dot{x}(t) &= A \dot{x}(t) + B \ddot{u}(t) \\
y(t) &= C \ddot{x}(t)
\end{align*}
\]

where

\[
\ddot{x}(t) = [L_d, L_q, V_{\text{cd}}, V_{\text{cq}}, V_{\text{cd}}, V_{\text{pq}}, i_L, V_{\text{qa}}]^T, \quad \ddot{u}(t) = [v_{\text{c}}, i_{\text{o}}]^T, \quad y(t) = v_{\text{o}},
\]

\[
A = \begin{bmatrix}
-\frac{1}{L_d} & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & -\frac{1}{L_q} & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & -\frac{1}{C_i} & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & -\frac{1}{C_i} & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & -\frac{4}{\pi C_p} & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & -\frac{1}{C_p} & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & -\frac{1}{C_p} & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & -\frac{1}{C_o}
\end{bmatrix}
\]

\[
C = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 1
\end{bmatrix}
\]

The aggregate linear model can also be represented using the transfer function technique

\[
v_{\text{o}}(s) = \begin{bmatrix} G_1(s) & G_2(s) \end{bmatrix} \begin{bmatrix} v_{\text{c}}(s) \\ i_{\text{o}}(s) \end{bmatrix}
\]

where

\[
G_1(s) \text{ is the control-to-output voltage transfer function}
\]

\[
G_2(s) = \frac{v_{\text{c}}(s)}{i_{\text{o}}(s)} = C(s L_{\text{o}} - A)^{-1} B
\]

\( B \) denotes row \( k \) column \( k \) of matrix \( B \).

**V. LINEARIZED CONVERTER MODEL ANALYSIS**

By considering the state-space model (36), Eigen values of the linearized system can be obtained by studying the complex s-plane. System Eigen values are obtained by (38), summarized in Table I, and plotted on the complex s-plane in Fig.9.

\[
|s L_{\text{o}} - A| = 0
\]

| Eigen Values for the Linearized Resonant Converter Model |
|---|---|---|
| Pole number | Pole location in complex s-plane | Pole natural frequency, \( \omega_n \) |
| \( P_{1,2} \) | \( \pm j \omega_s \) | \( \omega_s \) |
| \( P_{3,4} \) | \( S_{p_{3,4}} \) | \( \omega_{p_{3,4}} \) |
| \( P_{5,6} \) | \( S_{p_{5,6}} \) | \( \omega_{p_{5,6}} \) |
| \( P_{7,8} \) | \( -\frac{r_{L_d}}{2L_o} \pm j \sqrt{ \frac{1}{L_o C_o} - \frac{r_{L_o}^2}{4L_o^2} } \) | \( \frac{1}{\sqrt{L_o C_o}} \) |

*Defined in Appendix*
B. Control-to-output voltage transfer function

By comparing the weighted state feedback scheme in (33)-(34) with (31)-(32), at steady-state $v_{Cpd}$ is equal to the control input voltage $v_c$, i.e. $V_{Cpd}=V_c$. Then by examining Fig. 8, the control-to-output voltage transfer function $G_1(s)$ can be approximated by

$$ G_1(s) = \frac{v_c(s)}{v_s(s)} \approx \frac{2}{\pi} \frac{v_c(s)}{P_6(s)} \quad (39) $$

This can be derived from state-space equation (18) of the dc sub-system (output filter)

$$ G_1(s) = \frac{2}{\pi L C_s r_{cs} + r_{cs}} \quad (40) $$

Such a simplified second order control-to-output voltage transfer function is not to replace the derived model which provides detailed dynamics of the complete converter ac and dc state variables, but is useful for simplified closed loop PI control as in next subsection. In order to verify the validity of the approximated transfer function $G_1(s)$, Fig. 10 shows Bode plots and the step response comparing the behavior of the approximate control-to-output voltage transfer function with the exact transfer function $G_1(s)$ derived from (37).

![Fig. 9. Complex s-plane showing poles of the linearized resonant converter model.](image1)

![Fig. 10. Comparison between approximate and exact control-to-output voltage transfer function (a) Bode plots, and (b) step response.](image2)

![Fig. 11. Closed loop structure for output voltage control.](image3)

C. Closed loop design

Since the dc/dc series-parallel resonant converter is used as a voltage source, the main objective is output voltage control. Hence, output voltage is used for feedback in a single control loop. No right-half plane zeros exist in the control-to-output voltage transfer function, so there is no need for a multi-loop structure [44]. PI control can be used, due to the aggregate model derived where all the state variables are dc. This means an infinite loop gain can be achieved by placing a pole at the origin, thereby eliminating steady state error in the output voltage [45]. Fig. 11 shows the closed loop structure to be used for PI control design. $C(s)$ is PI control in a pole-zero form with $k_i$ as integral gain and $k_p$ as proportional gain. The location effect of the real left-hand plane zero $k_i/k_p$ is studied in Figs 12, 13 and 14 to select its best location for output response. The choice of $k_p$ determines system overall stability. Fig. 12 shows root locus diagrams for different $k_i/k_p$. Since the zero of the PI controller is placed on the real-axis, it is moved in relation to the real part of the complex output filter pole-pair ($\text{real}(P_{7,8})=r_{lo}/2L_o$). The more $k_i/k_p$ moves into the left hand plane, the more damped the closed loop poles for given $k_p$ and oscillations are less effective.
Although, for low values of \( k_i/k_p \), the closed loop stability margin is higher, however, system response is sluggish. Settling time cannot be reduced no matter how much \( k_p \) is increased. For this reason, high values of \( k_i/k_p \) are preferable for faster response though stability might be sacrificed due to a lower critical gain \( k_p \) for stability and lower phase margin. Fig. 13 shows the closed loop step response. Results confirm the slower rise and settling times with mitigated oscillations for higher \( k_i/k_p \). The step response is mainly over-damped since it is dominated by the low frequency real closed loop pole. Its natural frequency is lower than that of the complex pole pair. This is clear from the under-damped step response in Fig. 13(a) where \( k_i/k_p = 0 \). Fig. 14 shows the open loop Bode plots with different controller zero locations. As described by the root locus analysis, stability margin (phase margin) is reduced as \( k_i/k_p \) is increased. Usually a phase margin of 45° to 60° is sufficient to ensure adequate closed loop stability. High dc loop gain is ensured with the origin pole (integrator) which provides zero steady state error for the output voltage; an essential characteristic for a voltage source.

**D. Output Impedance**

Similar to the earlier analysis on the control-to-output voltage transfer function, the output impedance can be derived directly from the state-space model of the dc sub-system in (21). This is due to \( V_{cpd} = V_c \) at steady state. The output impedance transfer function \( G_2(s) \) is

\[
G_2(s) = \frac{V_c(s)}{I_c(s)} = \frac{I_s s + r_o}{L_s C_o s^3 + r_o C_o s^2 + \frac{1}{\pi} k_s \pi s + \frac{2}{\pi} \frac{k_i}{k_p}}
\]

The closed loop output impedance can be studied by examining Fig. 15(a) and is expressed by

\[
\frac{V_c(s)}{I_c(s)} = \frac{G_2(s)}{1 + C(s) G_2(s)} = \frac{\frac{L_s s + r_o}{L_s C_o s^3 + r_o C_o s^2 + \frac{1}{\pi} k_s \pi s + \frac{2}{\pi} \frac{k_i}{k_p}}}{1 + \frac{L_s C_o s^3 + r_o C_o s^2 + \frac{1}{\pi} k_s \pi s + \frac{2}{\pi} \frac{k_i}{k_p}}{L_s C_o s^3 + r_o C_o s^2 + \frac{1}{\pi} k_s \pi s + \frac{2}{\pi} \frac{k_i}{k_p}}}
\]

Fig.15(b) shows Bode plots for the open and closed loop output impedances. Any high frequency harmonic ripple in load current is attenuated by the converter output impedance. In dc/dc resonant converters, since the dominant frequency component of the load current is dc, open loop output impedance will result in a constant (voltage drop across \( r_{Lo} \)). This can be verified from the steady state gain in (41). For the closed loop, attenuation to the dc load current is achieved by the controller integrator, appearing as an origin-zero in (42). Higher \( k_i/k_p \) leads to greater attenuation and the closed loop has better disturbance rejection and robustness against load variations. Fig.15(c) shows the dynamic response of the closed loop voltage control to a step load change for different \( k_i/k_p \).
VI. SIMULATION AND EXPERIMENTAL IMPLEMENTATION

Fig. 16 illustrates the linearized SPRC closed loop output voltage control scheme, with the state feedback linearization scheme implemented. Closed loop output voltage control of a 40W, 40 kHz phase-controlled SPRC is implemented experimentally and simulated in Matlab with a detailed switching model to verify the accuracy and robustness of the derived model in equation (37). Outputs from the derived model (the calculated/estimated state variable values) are compared in Matlab with the detailed switching model of the converter and experimentally with actual converter measurements. Fig. 17 shows the control algorithm implementation both practically and in simulation and Table I summarizes the circuit and control parameter values.

Measurements of the actual SPRC output voltage ($v_o$) and output filter inductor current ($i_{Lo}$) are taken; the former to perform voltage control and the latter for state feedback linearization as shown in Fig 17(a) and (b). Since $i_{Lo}$ contains ripple due to the converter output filter, averaging is necessary since modeling of the dc subsystem (output filter) is based on an averaged state-space technique. Since the linearization scheme uses $v_{Cpq}=0$ and $i_{Brq}=0$, the $i_{Brd}$ necessary for the linearization scheme is obtained from $i_{Brd}=\frac{4\pi}{\pi}i_{Lo}$. The PI controller output $v_c$ and $i_{Brd}=\frac{4\pi}{\pi}i_{Lo}$ are inputs to the linearization scheme which calculates the necessary outputs $v_{ABd}$ and $v_{ABq}$ that force $v_{Cpq}=0$. The scheme is weighted by constants $k_1$, $k_3$, $k_5$ and $k_7$ which are based on the converter circuit parameters as defined by equation (25).

The phase shift angle $\delta$ between the inverter legs is then calculated by the algorithm in Fig. 17(c). With the state feedback outputs being $v_{ABd}$ and $v_{ABq}$ and knowing the supply voltage $v_s$ and transformer turns ratio $n$, the phase-shift angle can be calculated. All the inverter switches are switched with a fixed 50% duty cycle, the only control variable being the phase shift angle between $S_1$ and $S_3$ as shown in Fig. 17(d). This controls the effective inverter output voltage duty cycle. The phase-shift angle is updated every switching cycle (25µs), viz., the inverter is switched at 40 kHz.

Fig. 17. Closed loop control algorithm with state feedback implemented: (a) circuit diagram, (b) control algorithm, (c) phase-shift calculator, and (d) inverter phase control gating pattern.
In order to verify the linearized SPRC derived model, the state-space equation defining the system in (36) is discretized to estimate the converter state variables experimentally and in Matlab simulations. This allows the estimated results to be compared with measurements from the actual converter. The model is discretized with the main control algorithm interrupting at 25µs intervals, therefore, the sampling time used for discretization is \( T_s = 25 \mu s \). The discretized system is represented by

\[
\dot{x}(k+1) = A_d x(k) + B_d u(k)
\]

where

\[
A_d = e^{A T_s} = \frac{A T_s}{T_s}
\]

\[
B_d = \int A (T_s - \tau) B d \tau
\]

\[
\dot{x}(k) = \left[ i_{Ld(k)} i_{Lq(k)} v_{Csd(k)} v_{Csq(k)} v_{Cpd(k)} v_{Cpq(k)} v_{L0(k)} v_{o(k)} \right]
\]

\[
u = \left[ v_{Cc(k)} i_{Lp(k)} \right]
\]

\[i_o\] is the output (load) current which can be approximated by the average inductor current at steady state. Fig. 18 shows the typical sampling diagram for the control algorithm implementation using an Infineon TriCore 1796 DSP with C-code execution times for the various control algorithm parts summarized in Table III.

**Table II**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Internal resistance of resonant tank inductor ( r_{Ld} )</td>
<td>0.1916 ( \Omega )</td>
</tr>
<tr>
<td>Resonant tank inductance ( L_d )</td>
<td>0.1013 ( \mu H )</td>
</tr>
<tr>
<td>Parasitic transformer resistance referred to secondary ( r_t )</td>
<td>0.6 ( \Omega )</td>
</tr>
<tr>
<td>Transformer Leakage inductance referred to secondary ( L_t )</td>
<td>9.12 ( \mu H )</td>
</tr>
<tr>
<td>Total equivalent resistance ( r_e = r_t + r_{LS} )</td>
<td>0.7916 ( \Omega )</td>
</tr>
<tr>
<td>Total equivalent inductance ( L_e = L_t + L_s )</td>
<td>101.92 ( \mu H )</td>
</tr>
<tr>
<td>Resonant tank series capacitance ( C_s )</td>
<td>0.255 ( \mu F )</td>
</tr>
<tr>
<td>Resonant tank parallel capacitance ( C_p )</td>
<td>0.255 ( \mu F )</td>
</tr>
<tr>
<td>Internal resistance of output filter inductor ( r_{Lo} )</td>
<td>0.5 ( \Omega )</td>
</tr>
<tr>
<td>Output filter inductance ( L_o )</td>
<td>12.5 ( \mu H )</td>
</tr>
<tr>
<td>Output filter capacitance ( C_o )</td>
<td>120 ( \mu F )</td>
</tr>
<tr>
<td>Resonant tank fundamental frequency ( f_s )</td>
<td>40 ( kHz )</td>
</tr>
<tr>
<td>Supply voltage ( v_i )</td>
<td>60 ( V )</td>
</tr>
<tr>
<td>Transformer turns ratio ( n )</td>
<td>0.5</td>
</tr>
<tr>
<td>Full-load power rating of experimental test rig</td>
<td>40 ( W )</td>
</tr>
<tr>
<td>Characteristic impedance of resonant tank ( Z_s = \sqrt{L_s / C_s} )</td>
<td>20.7 ( \Omega )</td>
</tr>
<tr>
<td>Part-load resistive load ( R_{PL} )</td>
<td>40.5 ( \Omega )</td>
</tr>
<tr>
<td>Part-load Quality factor ( Q_{PL} = Z_s / R_{PL} )</td>
<td>0.511</td>
</tr>
<tr>
<td>Full-load resistive load ( R_{FL} )</td>
<td>14.4 ( \Omega )</td>
</tr>
<tr>
<td>Full-load Quality factor ( Q_{FL} = Z_s / R_{FL} )</td>
<td>1.44</td>
</tr>
<tr>
<td>PI controller parameters ( (P, I) = \delta (r_{Lo} / 2 L_o) )</td>
<td>100 ( Hz )</td>
</tr>
<tr>
<td>Proportional Gain ( k_p )</td>
<td>0.1</td>
</tr>
<tr>
<td>Integral Gain ( k_i )</td>
<td>10</td>
</tr>
<tr>
<td>Reference output voltage ( v_o^* )</td>
<td>24 ( V )</td>
</tr>
</tbody>
</table>

**Table III**

<table>
<thead>
<tr>
<th>Task</th>
<th>Execution time (( \mu s ))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fast ADC measurement</td>
<td>1</td>
</tr>
<tr>
<td>PI control loop</td>
<td>3</td>
</tr>
<tr>
<td>State feedback scheme</td>
<td>4</td>
</tr>
<tr>
<td>Phase shift calculation</td>
<td>2</td>
</tr>
<tr>
<td>State variables calculation/estimation</td>
<td>13</td>
</tr>
<tr>
<td>Total</td>
<td>23</td>
</tr>
</tbody>
</table>

### A. Model accuracy study

The response of the linearized large signal model to large signal variations is studied in order to assess its ability to track real converter behavior. A step reference voltage from \( v_o^* = 0 \) to \( v_o^* = 24 \( V \) \) is applied at \( t=0 \) and a step load change from part load (\( Q_{PL} = 0.511 \)) to full-load (\( Q_{FL} = 1.44 \)) is applied at \( t=5.0 \( s \) \). Simulation and experimental results are shown in Fig. 19 and 20 respectively. The experimental results illustrate actual converter measurements compared with calculated state variables using the derived model. The derived model uses equivalent dc quantities for the ac state variables of the resonant tank \( (i_{Ld}, v_{Cs} \text{ and } v_{Cp}) \). These quantities \( (i_{Ld}, i_{Lq}, v_{Csd}, v_{Csq}, v_{Cpd}, v_{Cpq}) \) do not actually exist, therefore, results compare the actual converter ac state variables measured with the corresponding peak value of the state variable calculated using the model. The peak values are calculated from the model using

\[
i_{Ld} = \sqrt{i_{Ld}^2 + i_{Lq}^2}
\]

\[
\sqrt{v_{Cs}^2 + v_{Csd}^2}
\]

\[
\sqrt{v_{Cpq}^2 + v_{Cpq}^2}
\]

For display purposes on an oscilloscope, these estimated state variables are pulse width modulated and filtered to obtain their analogue peak values and are compared to the converter ac state variables measurements.

With the application of two large signal variations (step reference voltage at \( t=0 \) and step load at \( t=5.0 \( s \) \)), the following can be deduced from Fig.19 and Fig. 20:

- The negligible differences between actual converter measurements and calculated state variables from the derived model verify the accuracy of the measured circuit parameters which the model depends on. Simulation and experimental results are closely matching.
- Calculated state variables track peak voltages and currents of the resonant tank as well as dc state variables of the output filter at steady state. However, slight variations occur in the transient response at the application of the large signal disturbance, especially in the voltage-based states \( v_o, v_{Cs} \) and \( v_{Cp} \) (Fig. 19(a), (d), (e) and Fig. 20(a), (c) and (d) respectively). This is because the model neglects, the ESR of the series-parallel resonant tank capacitors and the output filter capacitor. This is in order to avoid further model complication. Transient response of the current-based states such as \( i_L \) and \( i_{Lo} \) (Fig. 19(b) and (c) and Fig. 20(a) and (b) respectively) mimic the actual converter measurements.

![Fig.18 Sampling diagram](image-url)
Fig. 19. Matlab simulations comparing actual switching and proposed large signal model (full-load applied at $t=5.0s$), (a) output voltage, (b) output filter inductor current, (c) resonant tank inductor current, (d) resonant tank series capacitor voltage, (e) resonant tank parallel capacitor voltage, (f) dq equivalent resonant tank parallel capacitor voltages, (g) inverter output voltage at part-load and (h) inverter output voltage at full-load.
Fig. 20. Experimental results comparing measurements from the actual converter and the proposed large signal model, (a) output voltage and output filter inductor current, (b) resonant tank inductor current, (c) resonant tank series capacitor voltage, (d) resonant tank parallel capacitor voltage, (e) inverter output voltage at part-load (f) inverter output voltage at full-load

• Fig. 19(f) shows that the condition $v_{Cpq} = 0$ outlined in (30)-(35) is maintained by the state feedback linearization scheme at all operating conditions. Also, $v_{Cpq} = (\pi/2)v_o$. This verifies correct operation of the state feedback scheme.

• Fig. 19(g) and (h) and Fig. 20(e) and (f) show that after full load application ($Q_{FL} = 1.44$), the control loop increases the phase shift angle $\delta$ to produce more fundamental voltage output from the inverter. This is inevitable as the converter voltage gain is reduced as $Q$ increases, meaning more input voltage is required to maintain the required reference output voltage $v_o^* = 24V$.

• Natural increases occur in the values of $i_{LO}$ and $i_L$ after increased loading at $t=5.0s$. This causes an increased voltage drop on $v_{CS}$, whereas the increase in $v_{CP}$ is marginal. The latter can be explained by the fact that $v_{CP}$ controls $v_o$, so it is fairly constant with a slight increase to compensate for the increased voltage drop on the output filter inductor parasitic resistance after the application of full load at $t=5.0s$.

• The PI controller disturbance rejection capability can be improved to reduce the transient effect at the load transition instant. This can be performed by increasing the $k_i/k_p$ ratio but lower $k_p$ gain would need to be used to avoid closed loop instability, which means a more sluggish response.
B. Model Robustness study

Circuit parameters practically vary during operation. Resistive elements are affected by temperature and transformers and/or magnetic-core inductors are affected by core saturation. In order to assess the robustness of the derived model against such variations, a 10% increase in selected circuit parameters is applied to the actual switched converter model in simulation and compared with the unchanged parameter’s large signal model. Dominant circuit parameters that affect converter voltage gain are the resonant tank parasitic resistance $r_T$ and equivalent inductance $L_T$ which may be affected by changes in transformer leakage inductance. A 10% step increase in each parameter is applied to the converter operating at full load to assess the model’s response. The new parameter values applied are $r_T=0.87\,\Omega$ and $L_T=120\,\mu\text{H}$. Closed loop results for each case are taken separately and illustrated in Fig. 21.

The effect of changing $r_T$ is first studied. The actual converter’s behavior has negligible change at steady-state since the results for $v_o$ and $i_L$ are virtually unchanged after $t=1.5s$, as shown in Fig.21(a) and (b) respectively. The proposed model is capable of tracking the changed system...
parameter and estimates the state variables accurately. Fig. 21(c) confirms the minor effect on the converter due to changing $r_L$. This is shown by the analogous inverter output voltage $v_{AB}$ and $\delta$ compared to the original case of converter operation with unchanged $r_L$ as shown in Fig. 19(h).

The effect of changing $L_T$ is shown in Fig. 21(d)-(f). The increase in $L_T$ causes an increase in the resonant tank characteristic impedance. This causes a sudden drop in the output voltage $v_o$, and the control loop functions immediately in an attempt to correct this voltage sag by increasing the inverter output voltage via an increase of $\delta$ as shown in Fig. 21(f), when compared with Fig. 19(h). The output voltage is restored to the reference value after about 1.5s due to the increased circuit time constant with increased $L_T$. However, the model overestimates the output voltage by 5% due to the increased control input to the model. The resonant tank current $i_L$ decreases slightly (as in Fig. 21(e)) and similarly the model overestimates $i_L$ by 6%. It can be concluded that the model is relatively insensitive to changes in the resonant tank parasitic resistance $r_L$ whereas changing $L_T$ has more of an effect on the model’s performance. This is inevitable as the circuit resonant frequency changes and the entire dynamics of the converter are affected.

VII. CRITICAL EVALUATION

The original large signal non-linear model is an exact and precise representation of the converter for the whole load operating range. However, its non-linearity limits the application of simple and well known linear analysis and control techniques. Small signal models are an important linearization tool and have proven to be very successful for control design and stability analysis of many systems in the past. However the validity of the model remains limited in close neighbourhood of the steady state operating point and the model is not a true representative of large operational variations. From this perspective, the linearization scheme for the large signal model was proposed to preserve the large signal characteristics of the converter without linearizing around specific operating points. The methodology implemented for linearization can be merely viewed as an orientation of the ac subsystem dq state variables into an arbitrary reference frame to remove the main source of non-linearity; the mathematical “square root” function.

The proposed model has shown to provide closely matching results with the actual converter switched model. However, at high converter loading (high Q factor), the harmonic content in the resonant tank increases and the sinusoidal nature approximation of the resonant tank state variables becomes less accurate. This is mainly because a high Q factor means low load impedance compared to the resonant tank characteristic impedance. Consequently, the ratio of the injected square wave current from the bridge rectifier to the resonant circuit current is high, hence introducing higher order harmonics. Distortion introduced at high Q causes the proposed linearized model to have a marginal error in the value of the calculated state variables. This can be improved by assuming that resonant tank state variables are a harmonic series (instead of simply the fundamental component). However, this would result in n-times the existing number of resonant tank state variables, where n is the number of higher order harmonics included in the model. This makes the analysis way more difficult, tedious and increases the computation burden on the DSP and in return marginal improvement is achieved.

VIII. CONCLUSION

This paper proposes a feedback scheme that employs the output filter inductor current to obtain a linearized large signal model for the fixed-frequency phase-controlled SPRC. All state variables are converted to slow changing dc quantities which are easier to control than the fast resonant tank dynamics. The proposed state-space model represents converter behavior in response to large signal variations, and hence is useful for faster simulation in addition to estimating converter state variables for potential sensorless control applications. A reduced order transfer function was obtained to simplify the closed loop PI control design. PI control is sufficient to produce good closed loop dynamics and steady state performance. However, the limitation to increasing the proportional gain is the stability of the resonant tank. This can be improved by using multi-loop control. The model proved high accuracy when compared to the actual switching converter, and robustness against circuit parameter operational variation, especially changes in the resonant tank parasitic resistance. However, it is more sensitive to changes in the resonant tank inductance which is expected since the characteristic impedance and resonant frequency determining circuit behavior change accordingly.

APPENDIX

Parameters for Table II:

\[
S_{p_4} = \frac{-r_L}{2L_T} \pm j \sqrt{\frac{-r_L^2C_p + 4L_TC_s + 4L_T^2C_sC_p + 4L_T^2C_sC_p\omega_0^2 + 4L_T\omega_04L_T^2C_sC_p^2 + 4L_T^2C_sC_p^2 - r_L^2C_p^2C_s^2}{4L_T^2C_sC_p}}
\]
\[ S = -\frac{r}{2L'} + \frac{1}{j} \sqrt{-\frac{r^2C_p + 4L_pC_p + 4L_pC_p\omega^2 - 4L_p\omega\sqrt{4L_pC_pC_p^2 + 4L_pC_pC_p^2 - r^2C_pC_p^2}}{4L_p^2C_pC_p}} \]

\[ \omega_{\text{p}_{3,4}} = \sqrt{\frac{C_s + C_p + 4L_pC_p + L_pC_sC_p\omega^2 + \omega\sqrt{4L_pC_pC_p^2 + 4L_pC_p^2 - r^2C_p^2}}{L_pC_pC_p}} \]

\[ \omega_{\text{p}_{5,6}} = \sqrt{\frac{C_s + C_p + 4L_pC_p + L_pC_sC_p\omega^2 - \omega\sqrt{4L_pC_pC_p^2 + 4L_pC_p^2 - r^2C_p^2}}{L_pC_pC_p}} \]

REFERENCES


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